

50 HW (HL & SL) # 1, 3, 5

1.) $u_0 = 500$ $r = 1.12$

a.) i.) $500(1.12)^{10} \approx 1,552.92 \approx \boxed{1,553 \text{ ants}}$

ii.) $500(1.12)^{20} \approx 4,823.15 \approx \boxed{4,823 \text{ ants}}$

b.) $\frac{500(1.12)^n}{500} = \frac{2000}{500}$ $\log_{(1.12)}(4) = n$ $\approx \boxed{12.2 \text{ weeks}}$
 $(1.12)^n = 4$ $\approx 12.23 = n$

3.) $u_0 = 32$, $r = 1.18$ a.) i.) $32(1.18)^5 \approx 73.2 \approx \boxed{73 \text{ deer}}$

ii.) $32(1.18)^{10} \approx 167.4 \approx \boxed{167 \text{ deer}}$

b.) $\frac{5000}{32} = \frac{32(1.18)^n}{32} \Rightarrow 1.18^n = 156.25$ $\log_{1.18}(156.25) = n$

$n \approx 30.519 \approx \boxed{30.5 \text{ years}}$

5.) $r = 1 - 0.18 = 0.82$ $u_4 = 1.52$ $\therefore 1.52 = u_1(0.82)^4$
 $\Rightarrow \frac{1.52}{(0.82)^4} = \frac{u_1}{(0.82)^4}$
 $\Rightarrow \boxed{u_1 = 3.36 \text{ g}}$

b.) $\frac{0.2}{3.36} = \frac{3.36(0.82)^n}{3.36} \Rightarrow (0.82)^n = \frac{0.2}{3.36}$ $\Rightarrow \log_{0.82}\left(\frac{0.2}{3.36}\right) = n$

$\therefore n \approx 14.2$

$\therefore 14.2 - 4 = \boxed{10.2 \text{ years}}$