

Creating Linear Equations

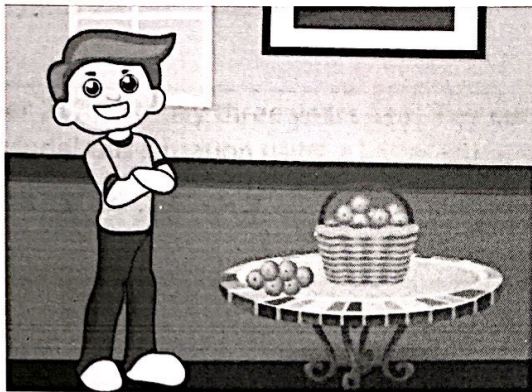
Opening Problem: Victor has 24 oranges – some in a basket, and 6 on the table. He is unsure of the number of oranges in the basket. How can this be represented in algebraic form?

X : # of oranges in basket

$$6 + X = 24$$

or

$$X = 24 - 6$$



$$\therefore X = 18$$

Vocabulary:

- **Equation:** an algebraic statement that equates two algebraic expressions by an equal sign.
- **Linear Equation:** an equation in which the highest power of the variable(s) is one.

Examples of Linear Equations

$$3x = 5$$

$$2x + y = 9$$

$$7a - 3b + 9c = 12$$

Verbal phrases can be translated into algebraic forms by identifying keywords. Some of them are given in the tables below:

Keywords	Operations
Plus Increased by More than	Addition
Minus Decreased by Less than	Subtraction
Times The product of Multiplied by	Multiplication
Divided Quotient of	Division

Other phrases	Symbol
- "in total"	- +
- "is the same as"	- =
- "a number"	- x
- "twice as much as"	- $2x$
- "per"	- x or \div

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Forming Linear Equations

Example 1: Four less than four times a number, N , is twelve. Translate the verbal phrase to algebraic form.

$$4x \quad x \rightarrow = 12$$

$$\boxed{4N - 4 = 12}$$

$$x = 2x \quad \checkmark$$

Example 2: Cindy celebrated her 25th birthday three years ago. Her current age is two times Fred's age. Model this situation using a linear equation.

Cindy's current age: $x = 25 + 3$

Fred's age: y

$$\therefore \boxed{25 + 3 = 2y}$$

$$\text{or} \quad \boxed{2y = 28}$$

$$+3 \quad = 1 + 2x$$

Example 3: Three years from now, Jenny's age will be one plus two times her current age. What is Jenny's current age?

Jenny's current age: x

$$x + 3 = 1 + 2x$$

$$-x \quad -x$$

$$3 = 1 + x$$

$$-1 \quad -1$$

$$\therefore \boxed{x = 2}$$

Example 4: Jalen went to the grocery store to get turkey, cheese, and bread for his lunches for the week. Turkey costs \$4.50 per pound, cheese costs \$2 per pound, and a loaf of bread is \$7.

a.) Write an equation to model the total cost of Jalen's trip to the grocery store.

lbs. of turkey: t

lbs. of cheese: c

loaf of bread: b

Total Cost: T

$$\boxed{T = 4.5t + 2c + 7b}$$

b.) If Jalen spent \$23.50 and purchased 3 pounds of turkey and one loaf of bread, how many pounds of cheese did he purchase?

$$23.50 = 4.5(3) + 2c + 7(1)$$

$$23.50 = 13.5 + 2c + 7$$

$$23.50 = 20.5 + 2c \quad c = 1.5$$

$$-20.5 \quad -20.5$$

$$\frac{3.00}{2} = \frac{2c}{2}$$

$$\boxed{1\frac{1}{2} \text{ pounds}}$$