

18F: 1aeim, 4abc, 7

$$1a.) y = \ln(7x) \rightarrow y' = \frac{7}{7x} = \boxed{\frac{1}{x}}$$

$$1e.) y = x^2 \ln x \quad u = x^2 \quad v = \ln x \quad y' = 2x \ln x + \frac{x^2}{x}$$
$$u' = 2x \quad v' = \frac{1}{x}$$
$$\boxed{y' = 2x \ln x + x}$$

$$1i.) y = \sqrt{\ln x} \quad y = u^{\frac{1}{2}} \quad u = \ln x$$
$$y' = \frac{1}{2\sqrt{u}} \quad u' = \frac{1}{x}$$
$$\boxed{y' = \frac{1}{2x\sqrt{\ln x}}}$$

$$1m.) y = \frac{2\sqrt{x}}{\ln x} \quad u = 2x^{\frac{1}{2}} \quad v = \ln x \quad \therefore y' = \frac{\ln x}{\sqrt{x}} - \frac{2\sqrt{x}}{(\ln x)^2}$$
$$u' = x^{-\frac{1}{2}} \quad v' = \frac{1}{x}$$
$$u' = \frac{1}{\sqrt{x}}$$
$$\Rightarrow \frac{\ln x - 2}{\sqrt{x}} \cdot \frac{1}{(\ln x)^2}$$

$$\Rightarrow \boxed{y' = \frac{\ln x - 2}{\sqrt{x}(\ln x)^2}}$$

$$4a.) y = \ln \sqrt{1-2x} \quad y = \ln u \quad u = \sqrt{1-2x} \quad y = \sqrt{u} \quad u = 1-2x$$

$$y' = \frac{1}{u} \cdot u' = \frac{1}{\sqrt{1-2x}} \cdot (-1) = \frac{-1}{\sqrt{1-2x} \cdot \sqrt{1-2x}} = \frac{-1}{1-2x} \Rightarrow \boxed{\frac{1}{2x-1}}$$

$$4b.) y = \ln \left(\frac{1}{2x+3} \right) \quad y = \ln u \quad u = (2x+3)^{-1} \quad y = u^{-1} \quad u = 2x+3$$

$$y' = \frac{1}{u} \cdot u' = \frac{1}{(2x+3)^{-1}} \cdot (-2) = \frac{-2}{(2x+3)^{-1} \cdot (2x+3)^2} = \frac{-2}{2x+3} \Rightarrow \boxed{y' = \frac{-2}{2x+3}}$$

$$4c.) y = \ln(e^x \sqrt{x}) \quad y = \ln u \quad u = e^x \sqrt{x} \quad u = e^x \cdot v = x^{\frac{1}{2}}$$

$$y' = \frac{1}{u} \cdot (u' = e^x \sqrt{x} + e^x \cdot \frac{1}{2\sqrt{x}}) = \frac{1}{e^x \sqrt{x}} \cdot (e^x \sqrt{x} + \frac{e^x}{2\sqrt{x}}) \Rightarrow \frac{e^x \sqrt{x}}{e^x \sqrt{x}} + \frac{e^x}{2\sqrt{x} e^x} \Rightarrow \boxed{1 + \frac{1}{2x}}$$

$$7.) f(x) = a \ln(bx^2) \quad f(e) = 3 \quad f'(1) = 6$$

$$\therefore 3 = a \ln(be^2) \quad f'(x) = \frac{2abx}{bx^2} \Rightarrow \frac{2a}{x}$$

$$\Rightarrow 3 = a[\ln b + \ln e^2] \quad \therefore 6 = \frac{2a}{1} \Rightarrow 6 = 2a \Rightarrow \boxed{a=3}$$

$$\text{plug in a} \quad \frac{3}{3} = \frac{3}{3} [\ln b + 2] \Rightarrow \ln b + 2 = 1 \quad \therefore e^{-1} = b$$

$$\ln b = -1 \quad \therefore \boxed{b = \frac{1}{e}}$$