

Name: Key

Algebra II

Period: _____

Homework: Solving Quadratics with Complex Roots

The Quadratic Formula

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

1

Write the equation in standard form, $ax^2 + bx + c$

2

Identify a, b, and c. Substitute them into the formula.

3

Simplify!

Directions: Solve each equation using the Quadratic Formula.

1.) $x^2 + 2x + 2 = 0$

$a=1 \quad b=2 \quad c=2$

$$\frac{-(2) \pm \sqrt{(2)^2 - 4(1)(2)}}{2(1)} \Rightarrow \frac{-2 \pm \sqrt{-4}}{2}$$

$$\Rightarrow \frac{-2 \pm 2i}{2} \Rightarrow \boxed{-1 \pm i}$$

2.) $x^2 + 4x + 8 = 0$

$a=1 \quad b=4 \quad c=8$

$$\frac{-(4) \pm \sqrt{(4)^2 - 4(1)(8)}}{2(1)} \Rightarrow \frac{-4 \pm \sqrt{-16}}{2}$$

$$\Rightarrow \frac{-4 \pm 4i}{2} \Rightarrow \boxed{-2 \pm 2i}$$

3.) $2x^2 + x + 5 = 0$

$a=2 \quad b=1 \quad c=5$

$$\frac{-(1) \pm \sqrt{(1)^2 - 4(2)(5)}}{2(2)} \Rightarrow \frac{-1 \pm \sqrt{-39}}{4}$$

$$\Rightarrow \boxed{\frac{-1 \pm i\sqrt{39}}{4}}$$

$\begin{array}{c} 39 \\ \diagdown \quad \diagup \\ 3 \quad 13 \end{array}$

4.) $3x^2 + 7x + 6 = 0$

$a=3 \quad b=7 \quad c=6$

$$\frac{-(7) \pm \sqrt{(7)^2 - 4(3)(6)}}{2(3)} \Rightarrow \frac{-7 \pm \sqrt{-23}}{6}$$

$$\Rightarrow \boxed{\frac{-7 \pm i\sqrt{23}}{6}}$$

5.) $x^2 + 7 = 2x$

$-2x \quad -2x$

$x^2 - 2x + 7 = 0$

$a=1 \quad b=-2 \quad c=7$

$$\frac{-(-2) \pm \sqrt{(-2)^2 - 4(1)(7)}}{2(1)} \Rightarrow \frac{2 \pm \sqrt{-24}}{2}$$

$$\Rightarrow \frac{2 \pm 2i\sqrt{6}}{2} \Rightarrow \boxed{1 \pm i\sqrt{6}}$$

$\begin{array}{c} 24 \\ \diagdown \quad \diagup \\ 4 \quad 6 \end{array}$

11.) $3x^2 + 5 = 4x + x^2$

$-x^2 - 4x + 4x + x^2 \quad 2x^2 - 4x + 5 = 0$

$a=2 \quad b=-4 \quad c=5$

$$\frac{-(-4) \pm \sqrt{(-4)^2 - 4(2)(5)}}{2(2)} \Rightarrow \frac{4 \pm \sqrt{-24}}{4}$$

$$\Rightarrow \frac{4 \pm -2i\sqrt{6}}{4} \Rightarrow \boxed{1 \pm \frac{i\sqrt{6}}{2}}$$

$\begin{array}{c} -24 \\ \diagdown \quad \diagup \\ 4 \quad 6 \end{array}$